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## About computing the nonlinear interaction between weakly converging sequences and its influence in optimal design and nonlinear elasticity

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### Abstract

When solving a calculus of variations problem, very often one encounters weakly converging sequences that interact in a nonlinear manner. Two paradigmatic examples of this are the broad area of optimal design, see [1], and the characterization of the energy density functions to be used in nonlinear elasticity. For the latter we present the use of Compensated Compactness, [6], to derive a computational method to look for the elusive counterexample of a rank-one, non quasiconvex energy density in the planar case, see [4] and [5]. In the context of optimal design we present the small amplitude homogenization approach introduced in [2] and used later in [3], which is based on the use of the technique of H-measures introduced by L. Tartar in [7], to compute the interaction between the design variable and the state function.

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